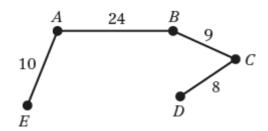
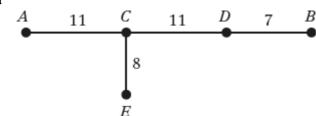
The travelling salesman problem 5B

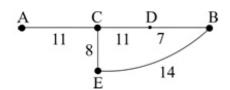
1 a Initial upper bound = 2×51 = 102



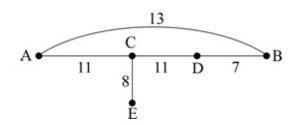
- **b** Use DE as a shortcut Route length = 51 + 28 = 79
- c Route ABCDEA length 79
- 2 a



- **b** Initial upper bound = $2 \times 37 = 74$
- **c** For example
 - i use BE as a shortcut



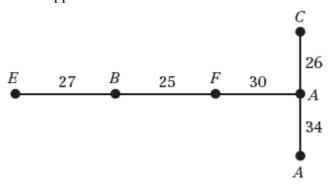
- or
- ii use AB as a shortcut



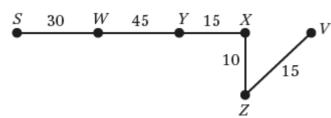
Other answers also possible

- **d** i Using BE route is A C E B D C A length 62
 - ii Using AB route is A C E C D B A length 58

3 a Initial upper bound = $2 \times 142 = 284$



- **b** Many possibilities: for example DE or EC or DF and EC
- c DE gives A C A F B E D A length 231 EC gives A D A F B E C A length 217 DF and EC gives A C E D F D A length 190
- 4 a



Initial upper bound = $2 \times 115 = 230$

- **b** For example arc VS
- c Route S W Y X Z V S length 190