

Further hypothesis tests 6C

1 a 2.34

b 3.36

c 3.37

2 a $\frac{1}{F_{8,6}} = 0.241$

b $\frac{1}{F_{12,25}} = 0.463$

c $\frac{1}{F_{5,5}} = 0.198$

3 a 3.37

b 4.20

c 6.06

4 a $\frac{1}{F_{12,3}} = 0.0370$

b $\frac{1}{F_{12,8}} = 0.176$

c $\frac{1}{F_{12,5}} = 0.101$

5 a 3.07, $\frac{1}{F_{10,8}} = 0.299$

b 2.91, $\frac{1}{F_{10,12}} = 0.364$

c 5.41, $\frac{1}{F_{5,3}} = 0.111$

6 $P(X < 0.5) = P(F_{40,12} < 0.5)$

$$= P\left(F_{12,40} > \frac{1}{0.5}\right)$$

$$= P(F_{12,40} > 2)$$

From the tables $F_{12,40}(0.05) = 2$

$$\therefore P(F_{12,40} > 2) = P(F_{40,12} < 0.5) = 0.05$$

$$\begin{aligned}7 \quad P(X < 3.28) &= 1 - P(F_{12,8} > 3.28) \\ &= 1 - 0.05 = 0.95\end{aligned}$$

$$\begin{aligned}P\left(X < \frac{1}{2.85}\right) &= P\left(F_{12,8} < \frac{1}{2.85}\right) \\ &= P(F_{8,12} > 2.85)\end{aligned}$$

$$\therefore P\left(X < \frac{1}{2.85}\right) = 0.05$$

$$\begin{aligned}P\left(\frac{1}{2.85} < X < 3.28\right) &= P(X < 3.28) - P\left(X < \frac{1}{2.85}\right) \\ &= 0.95 - 0.05 \\ &= 0.90\end{aligned}$$

$$\begin{aligned}8 \quad P(X < 9.55) &= 1 - P(F_{2,7} > 9.55) \\ &= 1 - 0.01 \\ &= 0.99\end{aligned}$$

$$\begin{aligned}9 \quad \mathbf{a} \quad P(X < 3.00) &= 1 - P(F_{6,12} > 3.00) \\ &= 1 - 0.05 = 0.95 \\ P(X > 0.25) &= P\left(F_{12,6} > \frac{1}{0.25}\right) \\ &= P(F_{12,6} > 4) \\ &= 0.05 \\ P(0.25 < X < 3) &= 0.95 - 0.05 \\ &= 0.90\end{aligned}$$

$$\mathbf{b} \quad {}^6C_2(0.9)^2(0.1)^4 \times 0.9 = 0.00109$$